# High-Speed Femto-Joule per Bit Silicon-Conductive Oxide Nanocavity Modulator

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Abstract—By combining the large Purcell effect of photonic crystal nanocavity and the strong plasma dispersion effect of the transparent conductive oxides, ultra-compact silicon modulators with heterogeneously integrated indium-tin-oxide (ITO) can potentially achieve unprecedented energy efficiency. In this article, we report the first high-speed silicon nanocavity modulator driven by an ITO gate, achieving 1.94 GHz bandwidth. On-off-key modulation is measured up to 3 Gb/s with only 2 V voltage swing and 18.3 fJ/bit energy efficiency. In addition, we perform in-depth analysis of the energy efficiency and high frequency simulation of the nanocavity modulator, revealing the critical role played by the semiconductor conduction path and the overlapping factor between the accumulated free carriers and the cavity resonant mode. Based on our analysis, we propose a strategy to further improve the modulation bandwidth to 23.5 GHz by node-matched doping and reduce the energy consumption to the range of hundreds of atto-joule per bit.

*Index Terms*—Electro-optic modulators, optical interconnec tions, optical resonators, photonic crystals, silicon photonics, transparent conductive oxides.

## I. INTRODUCTION

C ILICON photonics provides exclusive advantages for on-Chip optical interconnects in terms of bandwidth density, latency, energy efficiency, and cost effectiveness [1], [2]. Micro-resonators play pivotal rules in silicon photonic devices including high-speed and low-energy-consumption electrooptical (EO) modulators [3], [4], wavelength-division multiplex/demultiplex (WDM/DeMUX) modules [5], and chip-scale optical input/output (I/O) systems [6]. The light-matter interaction can be dramatically enhanced by utilizing a resonator structure such as micro-ring [3], [7], micro-disk [4], or photonic crystal (PC) nanocavity [8]-[10]. Compared with conventional Mach-Zehnder interferometer (MZI) modulators [11], resonator-based modulators offer remarkable reduction in device size and energy consumption, which can meet the stringent requirement of high density on-chip optical interconnects. Especially, as the bandwidth density of optical interconnect

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increases exponentially, the energy consumption per bit becomes the primary concern of the whole system. High energy efficiency of photonic devices can be achieved by increasing the Purcell factor of resonator modulators [12]. Among existing microresonators, PC nanocavity can offer much larger Purcell factor compared with micro-ring or micro-disk resonators [13] due to the ultra-compact mode volume. High Purcell factor resonator modulator is a promising path to simultaneously achieve high energy efficiency and large bandwidth as proved in previous studies [14].

In addition to the development of resonator-based E-O modulators, heterogeneous integration with other functional materials shows great promise to overcome the intrinsically weak plasma dispersion effect of silicon. It also provides the possibility to suppress the free carrier absorption by integrating high mobility semiconductor materials on the silicon platform. Various active materials such as III-V semiconductors [15], [16], 2D materials [17]–[19], transparent conductive oxides (TCOs) [9], [10], [20]–[24], LiNbO<sub>3</sub> [25], [26], and phase change materials [27], [28] have been integrated on silicon to build high performance photonic devices. In recent years, TCOs, such as indium-tin oxide (ITO), are attracting ever-increasing attention for EO photonic devices due to their strong plasma dispersion [29]. A compact ITO-based phase shifter has been demonstrated on silicon photonics to achieve an efficient  $V_{\pi}L$  of 0.52 V·mm [30]. The recently reported plasmonic enhanced versions of ITO-based phase shifters further improve the  $V_{\pi}L$  by another order of magnitude [31], [32]. Moreover, TCOs exhibit unique epsilon-near-zero (ENZ) effect in the telecom wavelength range [20]-[23], which can be used to enhance the free carrier absorption. Ultra-compact and broadband electro-absorption (EA) modulators using ENZ effect based on plasmonic slot waveguide [22], [23] and hybrid plasmonic-silicon waveguide structure [20], [21] have been demonstrated in recent years. Besides, moderately doped TCOs are electrically conductive but optically transparent, which makes them perfect gate materials for heterogeneous integration with silicon micro-resonators. Extremely large wavelength tunability of 250 pm/V has been demonstrated on both TCO-gated PC nanocavities [9], [10] and micro-ring resonators [24], which shows great potential for low-voltage and ultra-energy-efficient optical modulators and filters. Therefore, combining the large Purcell factor of PC nanocavity and the extremely large EO efficiency of TCO gate can potentially enable nanophotonic modulators with atto-joule/bit energy efficiency and high modulation bandwidth [10]. However, the modulation speed of previous TCO resonator modulators was limited to a

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few Mega-Hertz range due to the large series resistance and the lack of high-speed electrode design. Only TCO-based EA modulators achieved a data rate of 2.5 Gb/s at the cost of high driving voltage and energy consumption [21].

In this paper, we conducted holistic design of an ultracompact, high-speed PC nanocavity modulator driven by an ITO gate based on a silicon rib waveguide and high-speed coplanar electrodes. In-depth analysis of the energy efficiency and high frequency simulation of the nanocavity modulator reveals the critical role played by the semiconductor conduction path and the overlapping factor between the accumulated free carriers and the cavity resonant mode. To the best of our knowledge, this is the first systematic analysis of any high-speed TCO photonic devices. Experimentally, we achieved a 3-dB bandwidth of 1.94 GHz. Digital modulation using on-off-key (OOK) was measured up to 3 Gb/s with only 2 V voltage swing, which yielded an ultra-high energy efficiency of 18.3 fJ/bit. Moreover, we proposed a new method using node-matched doping and high-mobility TCO gate material, which can extend the modulation bandwidth to 23.5 GHz. Based on the quantitative analysis of the overlapping factor, we proposed a strategy to improve the energy efficiency to atto-joule per bit level.

### II. DESIGN AND FABRICATION

The working principle and fundamental device design of the PC nanocavity modulator has been described using fully etched silicon strip waveguide but can only operate at low E-O modulation speed [9], [10]. Fig. 1(a) shows the 3D schematic of the high-speed device design using silicon rib waveguide to achieve reduced series resistance in this work. The PC nanocavity consists of two back-to-back PC mirror segments on a silicon rib waveguide with 500 nm width and 250 nm height. The active region of the nanocavity modulator consists of an ITO/HfO<sub>2</sub>/Si MOS capacitor. The cross-sectional schematic is shown in Fig. 1(b). Here the 50 nm thick silicon slab waveguide serves as both the bottom of the MOS capacitor and electrical conduction path. The PC nanocavity is covered by 16 nm thick HfO<sub>2</sub> gate oxide layer. On top of that is the 20 nm thick ITO gate layer covering the center active region. When a negative bias is applied to the ITO gate, electrons and holes accumulate at both the ITO/ HfO2 and Si/ HfO2 interfaces, respectively. The accumulated free carriers induce blueshift of the resonance peak, modulating the light transmission. The relationship between resonance frequency detuning ( $\Delta \omega$ ) and accumulated free carriers can be described by the cavity perturbation theory [14]:

$$\frac{\Delta\omega}{\omega} = -\frac{\int \Delta\varepsilon |E|^2 dv}{2\int \varepsilon |E|^2 dv} = \frac{\alpha K Q_{tot}}{2V_m}.$$
(1)

Here,  $\omega$  are the resonance angular frequency of the nanocavity, E is the electric field distribution of the cavity mode,  $\varepsilon$  and  $\Delta \varepsilon$ are the initial and perturbed permittivity distribution. Because the plasma dispersion induced permittivity change  $\Delta \varepsilon$  is linear to the change of free carrier density  $\Delta N_c$ , the second term of (1) can be rewritten into the third term, where there are four major factors:  $K = -\partial (\Delta \varepsilon / \varepsilon) / \partial (\Delta N_c q)$  is the free carrier dispersion coefficient, which equals to the relative permittivity perturbation



Fig. 1. (a) 3D schematic of the ITO-gated silicon PC nanocavity modulator. (b) Cross-sectional schematic of the ITO/HfO<sub>2</sub>/Si MOS capacitor in the active region. The Si bottom and ITO gate contact pads are drawn on two sides of the waveguide for the ease of illustration. (c) Cross-sectional schematic of the silicon doping profile considered in the HFSS simulation. (d) Partial layout of the patterns used for the fabrication of the nanocavity modulator. (e) Equivalent circuit model of the PC nanocavity modulator in the active region.

per unit change of free carrier charge;  $Q_{tot}$  is the total change of the accumulated carrier charge;  $V_m = \int \varepsilon |E|^2 dv / \max(\varepsilon |E|^2)$ is the optical mode volume of the cavity mode; and  $\alpha$  is the overlapping factor that describes the overlapping between the free carrier perturbation and the electrical energy of the cavity mode, which can be expressed as:

$$\alpha = \frac{\int \Delta N_c q\varepsilon |E|^2 dv}{Q_{tot} \max(\varepsilon |E|^2)}.$$
(2)

In our previous publications [9], [10], [14], we have already discussed the advantages of the TCO-Si PC nanocavity modulator for achieving ultra-low energy consumption from perspectives of active material, optical resonator and capacitor design. However, in order to maximize the energy efficiency of the modulator, optimizing the overlapping factor  $\alpha$  is equally important. The overlapping factor determines the percentage of the electrically accumulated free carriers that can be used to interact with the light. A rigorous analysis of the overlapping factor requires to separately consider Si and ITO, since they have different free carrier dispersion coefficient K. However, to simplify the analysis, we focus our discussion on the average overlapping factor defined as  $\alpha_{ave} = (\alpha_{p-Si} + \alpha_{ITO})/2$ , where  $\alpha_{p-Si}$  and  $\alpha_{ITO}$  are the overlapping factors for the Si and ITO accumulation layer, respectively. Through the rest of this paper, the overlapping factor stands for this definition unless otherwise specified. Fig. 2(b) plots the top view of the normalized electrical energy density ( $\varepsilon |\mathbf{E}|^2/2$ ) distribution of the PC nanocavity



Fig. 2. (a) Overlapping factors vs. position of the ITO/HfO<sub>2</sub>/Si MOS capacitor by assuming the MOS capacitor covering 1 period of the PC nanocavity. (b) Top view of the electrical energy density distribution of the PC nanocavity. (c) and (d) Cross-sectional view of energy density distribution at (c)  $X = 0 \mu m$ and (d)  $Y = 0 \mu m$  with overlay of simulated free carrier density accumulation distribution at -2 V (blue shadow). Inset: Zoomed-in top view of nanocavity mode profile in the center period. Blue dashed lines label the cross-section positions of (c) and (d). Green dashed box labels the region where the overlapping factor reaches 22%.

simulated by 3D finite-difference time-domain (FDTD) using Lumerical FDTD, which corresponds to an ultra-compact optical mode volume of 0.058  $\mu$ m<sup>3</sup> (0.66( $\lambda$ /n<sub>Si</sub>)<sup>3</sup>). We can estimate the overlapping factor from the electrical energy distribution under the assumption of 1nm thick uniform accumulation layer. Fig. 2(a) plots the calculated overlapping factor versus the position of the active TCO-Si MOS capacitor by assuming the MOS capacitor covering one period of the PC nanocavity. Clearly, covering 3 periods of the PC nanocavity can provide a balance between energy efficiency and modulation speed. Fig. 2(c) and 2(d) show the cross-sectional electrical energy density distributions of the center period of the nanocavity modulator at positions  $X = 0 \ \mu m$  and  $Y = 0 \ \mu m$ , respectively, with overlays of accumulated free carrier distribution after applying -2 V bias on the ITO gate, which was simulated by Silvaco. We can directly visualize how the accumulated carriers are overlapped with the electrical energy. The overlapping factors of two cross

sections are calculated to be 6.28% and 24.3%, respectively. It is very clear that the subwavelength silicon bridge (72 nm wide) between air holes of the PC nanocavity helps to improve the overlapping factor.

For resonator-based E-O modulators, the modulation speed depends on two factors: the photon lifetime and the resistancecapacitance (RC) time delay constant. The overall 3 dB bandwidth can be calculated as  $f_{3\,dB} = 1/(1/f_{opt}^2 + 1/f_{RC}^2)^{1/2}$ . The photon-lifetime-limited bandwidth is on the order of  $f_{opt} =$ f/Q, where f is the resonance frequency and Q is the Q factor of the resonator. For PC nanocavity, the Q factor can be controlled by the air holes in the PC mirror segments [33] and the doping level. In this design, we target a Q factor of 5,000, which can support a bandwidth up to 38 GHz at 1.55  $\mu$ m wavelength. Therefore, the speed of the PC nanocavity modulator is majorly limited by the RC delay. However, a high capacitance density of the MOS capacitor is crucial to reduce the driving voltage and improve the energy efficiency [14]. Thus, it is especially important to reduce the series resistance in order to achieve both high-speed and high energy efficiency. The nanocavity modulator contains semiconductor conduction path through the silicon waveguide and thin ITO gate layer, which contribute to the majority of the series resistance. Thus, we optimized the electrical configuration, and reduced the resistance from both silicon and ITO. First, on the silicon side, the high-resistance silicon strip conduction path [10] is replaced by partially etched silicon slabs. Then, the doping of the silicon conduction path is carefully engineered. Fig. 1(d) shows the partial layout used for the fabrication of the nanocavity modulator. The 50 nm thick silicon slabs and the top 50nm-thick layer of the silicon waveguide (p+ region) are moderately doped, leaving the bottom 200nmthick layer of the silicon waveguide lightly doped (p-). The top 50nm-thick layer of the silicon contact area (p++ region) is highly doped and extends to only 500 nm away from the silicon waveguide edge. Fig. 1(c) illustrates the cross-sectional doping profile in this design. Next, on the ITO side, the length of the TCO conduction path is reduced by patterning the metal contact pad 1  $\mu$ m away to the nanocavity. In order to quantitatively evaluate the high-speed performance of the PC nanocavity modulator, we performed simulation of the modulator using ANSYS HFSS. The resistance and capacitance parameters are extracted according to the equivalent circuit model shown in Fig. 1(e). In the simulation, the dielectric constant of HfO2 has been adjusted to match the 8 fF/ $\mu$ m<sup>2</sup> capacitance density of the ITO/16nm HfO<sub>2</sub>/Si MOS capacitor simulated by quantum moment model [34]. We simulate both cases for the MOS capacitor covering the centric one and three periods of the PC nanocavity, which correspond to capacitances of 6.1 fF and 18.3 fF, respectively. The silicon series resistance can be divided into contributions from the three different doping regions (p-, p+, p++). Then, the total series resistance R can be expressed as:

$$R = R_{Si} + R_{ITO} = (R_{Si,p-} + R_{Si,p+} + R_{Si,p++}) + R_{ITO} + R_r$$
  
=  $R_{s,p-}A_{p-} + R_{s,p+}A_{p+} + R_{s,p++}A_{p++} + R_{s,ITO}A_{ITO}$   
+  $R_r$ . (3)

 TABLE I

 CIRCUITS PARAMETERS EXTRACTED FROM HFSS SIMULATION

	p-	p+	p++	ITO	R <sub>r</sub>
dopant density (cm <sup>-3</sup> )	$1 \times 10^{17}$	5×10 <sup>18</sup>	$1 \times 10^{20}$	2×10 <sup>20</sup>	١
Sheet resistance $(\Omega/\Box)$	10.7k (200nm)	2.9k (50nm)	253 (50nm)	625 (20nm)	١
Aspect ratio (3 perods)	0.08	0.18	0.9	0.892	١
$\begin{array}{c} R\left(\Omega\right)\\ (3 \ periods) \end{array}$	856	530	228	558	78
Aspect ratio (1 period)	0.08	0.22	0.55	3.19	١
$R(\Omega)$ (1 period)	856	638	139	1994	93

Here R<sub>s</sub> and A are the sheet resistance and the effective aspect ratio of different regions, and R<sub>r</sub> is the remaining resistance that cannot fit into the simplified linear resistance model. The effective aspect ratio is fitted by changing the sheet resistance of different regions. Detailed extracted parameters are listed in Table I. In our design, we choose doping concentrations of 1  $\times$  10<sup>17</sup> cm<sup>-3</sup>, 5  $\times$  10<sup>18</sup> cm<sup>-3</sup>, 1  $\times$  10<sup>20</sup> cm<sup>-3</sup> for p-, p+ and p++ regions of silicon, and  $2 \times 10^{20}$  cm<sup>-3</sup> carrier density for ITO. The corresponding S11 parameters from the HFSS simulation is plotted in Fig. 3(a). It gives us a total series resistance of  $\sim$ 3720  $\Omega$  and  $\sim$ 2250  $\Omega$  for 1 period and 3 periods coverage of the MOS capacitor, yielding RC-limited bandwidth of 7 GHz and 3.9 GHz, respectively. Fig. 3(b) shows the normalized voltage across the MOS capacitor  $V_{MOS}$  as a function of frequency by assuming 1 V at the signal input. It equals to 2 V at low frequency due to the signal reflection. We have verified the electrical configuration with FDTD simulation that with such doping we can still achieve a O factor of  $\sim$ 5,000.

The nanocavity modulator is fabricated on a 250 nm thick lightly doped p-type silicon-on-insulator (SOI) substrate. First, the waveguide and PC nanocavity are patterned by electronbeam lithography (EBL), followed by reactive ion etching (RIE) of 200 nm thickness into the silicon, leaving a 50 nm thick Si slab for conduction and PC nanocavity with partially etched air holes. The grating couplers are pattern by a second round of EBL and RIE. Then, the p+ region and p++ region is selectively implanted with 5 keV B+ ions at flux of 2.5  $\times$   $10^{13}~\text{cm}^{-2}$  and 6  $\times$   $10^{14}~\text{cm}^{-2}$  with tilted angles of 7° and 30°, respectively. After the ion implantation, the dopants are activated by rapid thermal annealing at 1000 °C for 10 seconds. Next, 16nm thick HfO<sub>2</sub> layer is deposited using atomic layer deposition (ALD). After the ALD, the oxide at the silicon contact region is removed by buffered hydrofluoric acid. Ni/Au coplanar ground-signal-ground (GSG) electrode pads are patterned by contact photolithography, thermal evaporation and lift-off. Finally, the Au contact pads under the ITO and the ITO gate layer are patterned by EBL and lift-off. 20 nm of ITO gate layer is sputtered at 1% O2/Ar gas flow, which yields an ITO resistivity of  $\sim 1.4 \times 10^{-3} \ \Omega \cdot cm$ . The fabricated device is shown in Fig. 4(a) and 4(b), which occupies a total footprint of  $0.091 \text{ mm}^2$ , including  $0.077 \text{ mm}^2$  of GSG electrodes,  $0.014 \text{ mm}^2$ 



Fig. 3. (a) S11 parameters from the HFSS simulation. Inset: circuit model used to fit the S11 parameters.  $C_{pad}$  is the parasitic capacitance between the contact pads. (b) Normalized voltage across the MOS capacitor as a function of frequency.

of metal-semiconductor contact pads, and a compact photonic device area of 43  $\mu$ m<sup>2</sup>. The photonic device area includes a 14.8  $\mu$ m long PC nanocavity with 22 air holes in each PC mirror segments and 1.2  $\mu$ m wide partially etched silicon slabs on both sides of the cavity. The length of the ITO gate is 1  $\mu$ m, which covers the centric three periods of the PC nanocavity as shown in Fig. 4(c). We should point out that the sizes of the metal-semiconductor contact pads are limited by the precision of the contact photolithography, which can be reduced to comparable to the photonic device area with more sophisticated fabrication process.

## **III. EXPERIMENT RESULTS**

The fabricated devices are characterized with light input and output via surface grating couplers. A polarization controller is used to excite the transverse electric (TE) mode light. The PC nanocavities are designed to operate at C-band. Fig. 5(a) shows the transmission spectra of a fabricated nanocavity modulator with resonance wavelength at 1538 nm and the corresponding passive PC nanocavity. The plotted transmission spectra are normalized to that of a straight waveguide with the same grating couplers. The fabricated modulator exhibits a Q factor of ~5,600 and insertion loss (IL) of 7.8 dB. Before ITO gate deposition and Si doping, the Q factor and IL of the passive PC nanocavity is



Fig. 4. (a) Optical image of the fabricated PC nanocavity modulator. (b) Zoomed-in optical image of the nanocavity modulator at the active region (dashed box in (a)). (c) Colored scanning electron micrograph (SEM) of the active region of the modulator.



Fig. 5. (a) Normalized transmission spectra of a fabricated PC nanocavity modulator and the corresponding passive PC nanocavity modulator (before Si doping and ITO gate deposition). Optical losses extrinsic to the device, such as grating couplers, are subtracted from the data. (b) Normalized transmission spectra of the PC nanocavity modulator at different bias voltage.

measured to be 9,460 and 7.66 dB, respectively. The free carrier absorption of the doped Si and ITO gate reduced the Q factor significantly while only slightly increases the IL, indicating that the passive nanocavity quality is the limiting factor for the current IL. Considering a low IL of 1 dB has been demonstrated by other researchers using the same PC nanocavity design principle [8], we anticipate that the IL of the TCO-Si PC nanocavity modulator can be significantly reduced by improving the side wall smoothness, the air hole uniformity, and compensating the pattern distortion during the lithography and etching process with more advanced fabrication processes.

Fig. 5(b) shows the transmission spectra of the modulator at different bias voltages. With -4 V applied bias, the peak resonance wavelength shifts 284 pm, corresponding to a wavelength tunability of 71 pm/V. At -2 V bias, a peak extinction ratio (ER) of 3.45 dB can be reached. The wavelength tunability is less than the previous demonstration [10] due to two reasons. First, the HfO<sub>2</sub> gate oxide layer is thicker than the previous case, which results in smaller capacitance density of the MOS capacitor. Second, limited by the alignment accuracy of our EBL instrument, we have to pattern and etch the air holes and silicon slabs in the same step of fabrication process. This leads to under etching of air holes due to the local loading effect of the RIE [35]. As a result, the real overlapping factor is smaller than the previous ideal estimation, since more optical field is contained inside the silicon waveguide slab. The overlapping factor can be esimated as

$$\alpha = \frac{\Delta\lambda}{V} \frac{V_m}{\lambda \cdot K_{ave} \cdot C},\tag{4}$$

Where  $\Delta \lambda / V$  is the wavelength tunability,  $\lambda$  is the resonance wavelength, and C is the capacitance. The average free carrier dispersion coefficient  $K_{ave}$  is defined as  $K_{ave} =$  $(\alpha_{Si}K_{Si} + \alpha_{ITO}K_{ITO}) / (\alpha_{Si} + \alpha_{ITO})$ . According to our simulation (Fig. 2(a)), the overlapping factor of silicon accumulation layer  $\alpha_{p-Si}$  is 2~2.6 × larger than that of ITO  $\alpha_{ITO}$ due to more optical energy is confined in the silicon region. Then, we can estimate the  $K_{ave}$  as  $0.7K_{Si} + 0.3K_{ITO}$ , to be  $\sim$ 7.4  $\times$  10<sup>-3</sup> C·cm<sup>3</sup> [14]. Next, we can calculate the actual overlapping factor to be 1.96%. As a comparison, our previous demonstration achieved a wavelength tunability of 250 pm/V with 1 period coverage of the MOS capacitor and an overlapping factor of 8.13%, which is very close to the overlapping estimation in the previous section. Therefore, optimizing the fabrication processes to achieve a similar overlapping factor for high speed E-O modulators is still necessary for future research.

The high-speed response of the nanocavity modulator is measured using the setup shown in Fig. 6(a). The AC signal is generated by Anritsu MP1763B and combined with a DC bias through a bias tee before applying to the device through a high-speed probe (Infinity Probe). The output optical signal is measured by a digital communications analyzer (Agilent 86100A). Fig. 6(b) plots the AC EO modulation at 1.25 GHz with  $2 V_{\rm pp}$  rectangular voltage swing. The asymmetric waveform is due to the dynamics of resonator based modulator [36]. The 10-90 rise and fall times of the optical response are measured to be  $\sim 0.135$  ns and  $\sim 0.18$  ns, respectively. Then, the RC time constant  $\tau_{\rm RC}$  and the 3-dB bandwidth  $f_{\rm 3dB}$  of the modulator can be calculated based on the slower transition edge (falling edge) as  $\tau_{RC} = t_{\text{fall}} / \ln(\frac{0.9}{0.1}) = t_{\text{fall}} / 2.2$  and  $f_{3\text{dB}} = 1/2\pi\tau_{RC} =$  $0.35/t_{\rm fall}$  to be 82 ps and 1.94 GHz, respectively. Assuming the capacitance of 18.3 fF from the previous simulation, we can calculate the series resistance of the nanocavity modulator to be



Fig. 6. (a) Schematic of the AC testing setup. (b) Electrical input and optical output AC modulation signal at 1.25 GHz with 2  $V_{\rm pp}$  voltage swing. (c) Measured signals at 3 Gb/s.

~4.5 k $\Omega$ . The ITO conduction path contributes ~0.6 k $\Omega$  to the series resistance, which can be calculated from the ITO sheet resistance. Then, ~3.9 k $\Omega$  comes from the silicon conduction path, which also matches the estimation from the resistance between the two ground electrode pads. Overall, the experiment result matches well with the HFSS simulation. Besides, the sheet resistance of the p++ region on the device chip is measured to be ~1100  $\Omega/\Box$ , which indicates that the larger resistance from the silicon conduction path may be due to inaccurate implantation conditions or partial activation of the dopants, and the induced large contact resistance. Finally, we measured the high-speed digital modulation of the nanocavity modulator up to 3 Gbps. Fig. 6(c) shows the measured signals at 3 Gbps data rate. The asymmetric shape of the signal is due to the input driven signal we used for the measurement, as is shown in the inset of Fig. 6(c).

# IV. STRATEGIES FOR HIGHER MODULATION BANDWIDTH AND ATTO-JOULE PER BIT ENERGY EFFICIENCY

We have proved the capability of the gigahertz operation of the TCO-Si PC nanocavity modulator, which matches the prediction of our design and simulation. Here, we discuss how we can further improve the modulation speed. Basically, the series resistance from both the silicon and ITO need to be reduced. On the silicon side, the series resistance can be further reduced using node-matched doping technique [37]. Such method allows us to put the p++ doping region closer to the active cavity region without significantly affecting the optical mode as is illustrated in Fig. 7(a). FDTD simulation also gives us a Q factor larger than 5,000. On the gate side, by replacing ITO ( $\mu =$  $20 \text{ m}^2/(\text{Vs})$ ) with high mobility TCO materials such as Ti-doped In<sub>2</sub>O<sub>3</sub> ( $\mu$ >80 m<sup>2</sup>/(Vs)) [38], the TCO series resistance can be reduced by more than 4×. In the meantime, larger mobility also



Fig. 7. (a) Layout schematic of node-matched doping profile with overlay of the electrical energy density distribution. (b) Cross-sectional schematic for building TCO-Si MOS capacitor over the subwavelength Si bridge through making window on the top cladding layer.

induces less plasma absorption. We simulated the resistance of the proposed structure. It yields a total series resistance of less than 852  $\Omega$ , which leads to a RC bandwidth of 30 GHz for 1 period coverage of MOS capacitor. The overall 3 dB bandwidth reaches over 23.5 GHz. Such optimized nanocavity modulator can be modulated at 40 Gbps using simple OOK for on-chip optical interconnects.

The energy consumption of this PC nanocavity modulator can be calculated as CV<sup>2</sup>/4, to be 18.3 fJ/bit by assuming 2  $V_{pp}$ . However, we anticipate that larger wavelength tunability, smaller driving voltage, and higher energy efficiency can be achieved. For example, 262 pm/V wavelength tunability should be achievable by increasing the overlapping factor from 1.95% to 7.2%. Based on the Q factor and capacitance of current device, the driving voltage can be reduced to 0.54 V, leading to energy consumption of 1.33 fJ/bit. Furthermore, as discussed in Section II, the subwavelength silicon bridge between air holes exhibits much larger overlapping factor than the overall PC nanocavity. By principle, we can build the active TCO-Si MOS capacitor only at the subwavelength bridge region, for example, through making a window on top of the cladding layer as shown in Fig. 7(b). Assuming we can increase the overlapping factor from 7.2% to  $\sim$ 22%, which corresponds to a 100 nm long region of the silicon subwavelength bridge (green dashed box in inset of Fig. 2(d)), we can further reduce the required capacitance by nearly  $3 \times$  to 6 fF, while not sacrificing the wavelength tunability. In that case, the energy consumption can potentially be reduced to 437 aJ/bit.

Finally, we briefly compare the energy efficiency of our TCO-Si PC nanocavity modulator with other silicon resonatorbased E-O modulators based on different resonator designs and capacitors. The energy consumption of a resonator-based modulator is dependent on four main factors [14]: the carrier dispersion coefficient K of the active material, the Purcell factor of the resonator  $F_P$ , the total capacitance C, and the overlapping factor  $\alpha$ . The comparison of these devices is listed in Table II We can see that there are two main advantages of the TCO-Si PC nanocavity modulator. First, the small mode volume of PC nanocavity helps to achieve large Purcell factors. For high-speed resonator-based modulators, the Q factor is typically limited to only a few thousand, due to photon-lifetime bandwidth consideration. Then, a small mode volume becomes especially

TABLE II COMPARISON OF SILICON RESONATOR-BASED MODULATORS

Ref	Capacitor	$V_{m}$	$gF_{p}{}^{a}$	С	α	$E_{\text{bit}}$
	/resonator type	$((\lambda/n_{Si})^3)$		(fF)		(fJ/bit)
[41]	vertical PN		166	20	12.2%	
	junction /micro-	4.46				61
	disk					
[4]	vertical PN		146. 5	17	100%	1
	junction /micro-	6.82				
	disk					
[7]	lateral PN		87.5	50	15.6%	50
	junction /micro-	36.29				
	ring					
[42]	Si/oxide/Si					
	MOS	21.20	28	320	10.5%	180
	/micro-ring					
[43]	interleaver					
	PN junction	105.74	29	66	36.9%	66
	/micro-ring					
[10]	hybrid Si-ITO		855		8.13%	3.25
	MOS /PC	0.55		13		
	nanocavity					
proposal	hybrid Si-ITO					
in this	MOS /PC	0.66	1247	6	22%	0.437
paper	nanocavity					

<sup>a</sup>Purcell factor F<sub>P</sub> is defined as  $F_P = (3/4\pi^2)(\lambda n)^3 (QV_m)$ . Detune factor g is defined as the ratio between the the full width at half maximum (FWHM) of the resonator to the required resonance detuning of the modulator.

important. In this work, we achieve a Purcell factor of PC nanocavity almost an order of magnitude larger than that of mico-disk modulators. Second, the large capacitance density and design freedom of the MOS capacitor help us to achieve a reasonable capacitance in a miniaturized active device volume. The main drawback of the TCO-Si hybrid PC nanocavity modulator is the relatively small overlapping factor. The carrier accumulation of MOS capacitors occurs at the interfaces of the waveguide, while the perturbation of free carriers of reversed biased PN junction is inside the waveguide, which intrinsically has better overlapping with the optical mode. For example, the overlapping factor of our previous PC nanocavity modulator is more than one order of magnitude smaller than that of a vertical PN junction micro-disk modulator [4], which reaches a perfect overlapping of 100%. Luckily, the overlapping factor of the TCO-Si hybrid PC nanocavity modulator can be further optimized by taking advantage of the subwavelength structure of PC nanocavities as discussed here. Besides, further reducing the energy consumption can also possibly be achieved by adapting PC nanocavities with more miniaturized cavity mode volume, such as slot PC cavities [39] or bowtie PC cavities [40]. In summary, TCO-Si PC nanocavity modulator offers us the best possibility to achieve both high-speed operation and extremely low energy consumption at hundreds of atto-joule per bit level simultaneously. However, significant engineering optimization is still needed to achieve such ultimate goals.

# V. CONCLUSION

In summary, we presented comprehensive design and in-depth analysis of an ultra-compact, high-speed TCO-Si PC nanocavity modulator based on ITO/HfO<sub>2</sub>/Si MOS capacitor. We quantitatively analyzed the overlapping factor between the accumulated free carriers and the cavity resonant mode. Its contribution to the energy efficiency of the modulator is sufficiently discussed. The relationship between the doping of semiconductor conduction path and modulation speed was systematically investigated via high frequency simulation. In our experimental demonstration, the fabricated TCO-Si nanocavity modulator shows a wavelength tunability of 71 pm/V with a Q factor of  $\sim$ 5,600, achieving 3.45 dB ER with 2  $V_{pp}$  applied bias. We demonstrated a 3 dB modulation bandwidth of 1.94 GHz. E-O modulation was measured up to 3 Gb/s with 2  $V_{\rm pp}$  voltage swing, which corresponds to an energy efficiency of ~18.3 fJ/bit. Besides, we proposed that the series resistance can be further reduced by node-matched doping of Si and high-mobility TCO material, which can improve the 3 dB bandwidth to over 23.5 GHz. Furthermore, based on the quantitative analysis of the overlapping factor, we predict that single-digit femto-joule per bit energy efficiency of 1.33 fJ/bit can be reached through optimizing the gate oxide thickness and fabrication processes. Further increasing the overlapping factor is possible through precisely covering the TCO-Si MOS capacitor at the subwavelength silicon bridge of PC nanocavity. With that, an extremely low energy consumption of 437 aJ/bit can be achieved. As the first systematic analysis and experimental demonstration of high-speed Si-TCO resonator-based modulator, this work directly proves the potential of TCO-gated silicon photonic devices for high density, high-speed, ultra-low energy optical interconnect systems.

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#### REFERENCES

- I. A. Young et al., "Optical I/O technology for tera-scale computing," IEEE J. Solid-State Circuits, vol. 45, no. 1, pp. 235–248, Jan. 2010.
- [2] D. A. B. Miller, "Optical interconnects to silicon," *IEEE J. Sel. Top. Quantum Electron.*, vol. 6, no. 6, pp. 1312–1317, Nov. 2000.
- [3] J. Sun, R. Kumar, M. Sakib, J. B. Driscoll, H. Jayatilleka, and H. Rong, "A 128 Gb/s PAM4 silicon microring modulator with integrated thermooptic resonance tuning," *J. Lightw. Technol.*, vol. 37, no. 1, pp. 110–115, Jan. 2019.
- [4] E. Timurdogan, C. M. Sorace-Agaskar, J. Sun, E. Shah Hosseini, A. Biberman, and M. R. Watts, "An ultralow power athermal silicon modulator," *Nat. Commun.*, vol. 5, no. 1, Dec. 2014, Art. no. 4008.
- [5] L.-W. Luo *et al.*, "WDM-compatible mode-division multiplexing on a silicon chip," *Nat. Commun.*, vol. 5, no. 1, May 2014, Art. no. 3069.
- [6] A. H. Atabaki *et al.*, "Integrating photonics with silicon nanoelectronics for the next generation of systems on a chip," *Nature*, vol. 556, no. 7701, pp. 349–354, Apr. 2018.
- [7] P. Dong et al., "Low V\_pp, ultralow-energy, compact, high-speed silicon electro-optic modulator," Opt. Express, vol. 17, no. 25, Dec. 2009, Art. no. 22484.
- [8] A. Shakoor, K. Nozaki, E. Kuramochi, K. Nishiguchi, A. Shinya, and M. Notomi, "Compact 1D-silicon photonic crystal electro-optic modulator operating with ultra-low switching voltage and energy," *Opt. Express*, vol. 22, no. 23, Nov. 2014, Art. no. 28623.

- [9] E. Li, Q. Gao, R. T. Chen, and A. X. Wang, "Ultracompact siliconconductive oxide nanocavity modulator with 0.02 lambda-cubic active volume," *Nano Lett.*, vol. 18, no. 2, pp. 1075–1081, 2018.
- [10] E. Li, Q. Gao, S. Liverman, and A. X. Wang, "One-volt silicon photonic crystal nanocavity modulator with indium oxide gate," *Opt. Lett.*, vol. 43, no. 18, Sep. 2018, Art. no. 4429.
- [11] J. Ding, R. Ji, L. Zhang, and L. Yang, "Electro-optical response analysis of a 40 Gb/s silicon Mach–Zehnder optical modulator," *J. Lightw. Technol.*, vol. 31, no. 14, pp. 2434–2440, 2013.
- [12] D. A. B. Miller, "Attojoule optoelectronics for low-energy information processing and communications," *J. Lightw. Technol.*, vol. 35, no. 3, pp. 346–396, Feb. 2017.
- [13] K. J. Vahala, "Optical microcavities," *Nature*, vol. 424, no. 6950, pp. 839–846, Aug. 2003.
- [14] E. Li and A. X. Wang, "Theoretical analysis of energy efficiency and bandwidth limit of silicon photonic modulators," J. Lightw. Technol., vol. 37, no. 23, pp. 5801–5813, Dec. 2019.
- [15] T. Hiraki et al., "Heterogeneously integrated III-V/Si MOS capacitor Mach–Zehnder modulator," Nat. Photon., vol. 11, no. 8, pp. 482–485, Aug. 2017.
- [16] J.-H. Han, F. Boeuf, J. Fujikata, S. Takahashi, S. Takagi, and M. Takenaka, "Efficient low-loss InGaAsP/Si hybrid MOS optical modulator," *Nat. Photon.*, vol. 11, no. 8, pp. 486–490, Jul. 2017.
- [17] M. Liu *et al.*, "A graphene-based broadband optical modulator," *Nature*, vol. 474, no. 7349, pp. 64–67, Jun. 2011.
- [18] V. Sorianello *et al.*, "Graphene-silicon phase modulators with gigahertz bandwidth," *Nat. Photon.*, vol. 12, no. 1, pp. 40–44, Jan. 2018.
- [19] Z. Sun, A. Martinez, and F. Wang, "Optical modulators with 2D layered materials," *Nat. Photon.*, vol. 10, no. 4, pp. 227–238, Apr. 2016.
- [20] V. J. Sorger, N. D. Lanzillotti-Kimura, R. M. Ma, and X. Zhang, "Ultracompact silicon nanophotonic modulator with broadband response," *Nanophotonics*, vol. 1, no. 1, pp. 17–22, Jan. 2012.
- [21] M. G. Wood *et al.*, "Gigahertz speed operation of epsilon-near-zero silicon photonic modulators," *Optica*, vol. 5, no. 3, Mar. 2018, Art. no. 233.
- [22] H. W. Lee *et al.*, "Nanoscale conducting oxide PlasMOStor," *Nano Lett.*, vol. 14, no. 11, pp. 6463–6468, Nov. 2014.
- [23] Q. Gao, E. Li, and A. X. Wang, "Ultra-compact and broadband electroabsorption modulator using an epsilon-near-zero conductive oxide," *Photon. Res.*, vol. 6, no. 4, Apr. 2018, Art. no. 277.
- [24] E. Li, B. A. Nia, B. Zhou, and A. X. Wang, "Transparent conductive oxidegated silicon microring with extreme resonance wavelength tunability," *Photon. Res.*, vol. 7, no. 4, Apr. 2019, Art. no. 473.
- [25] A. J. Mercante, P. Yao, S. Shi, G. Schneider, J. Murakowski, and D. W. Prather, "110 GHz CMOS compatible thin film LiNbO<sub>3</sub> modulator on silicon," *Opt. Express*, vol. 24, no. 14, Jul. 2016, Art. no. 15590.
- [26] L. Chen, Q. Xu, M. G. Wood, and R. M. Reano, "Hybrid silicon and lithium niobate electro-optical ring modulator," *Optica*, vol. 1, no. 2, Aug. 2014, Art. no. 112.
- [27] J. T. Kim, "CMOS-compatible hybrid plasmonic modulator based on vanadium dioxide insulator-metal phase transition," *Opt. Lett.*, vol. 39, no. 13, Jul. 2014, Art. no. 3997.
- [28] K. J. A. Ooi, P. Bai, H. S. Chu, and L. K. Ang, "Ultracompact vanadium dioxide dual-mode plasmonic waveguide electroabsorption modulator," *Nanophotonics*, vol. 2, no. 1, pp. 13–19, Jan. 2013.
- [29] E. Feigenbaum, K. Diest, and H. A. Atwater, "Unity-order index change in transparent conducting oxides at visible frequencies," *Nano Lett.*, vol. 10, no. 6, pp. 2111–2116, Jun. 2010.
- [30] R. Amin et al., "0.52 v mm ITO-based Mach–Zehnder modulator in silicon photonics," APL Photon., vol. 3, no. 12, Aug. 2018, Art. no. 126104.
- [31] R. Amin et al., "A lateral MOS-capacitor-enabled ITO Mach–Zehnder modulator for beam steering," J. Lightw. Technol., vol. 38, no. 2, pp. 282–290, 2020.
- [32] R. Amin *et al.*, "Sub-wavelength GHz-fast broadband ITO Mach–Zehnder modulator on silicon photonics," *Optica*, vol. 7, no. 4, Apr. 2020, Art. no. 333.
- [33] Q. Quan and M. Loncar, "Deterministic design of wavelength scale, ultrahigh Q photonic crystal nanobeam cavities," *Opt. Express*, vol. 19, no. 19, Sep. 2011, Art. no. 18529.
- [34] Q. Gao, E. Li, and A. X. Wang, "Comparative analysis of transparent conductive oxide electro-absorption modulators [Invited]," *Opt. Mater. Express*, vol. 8, no. 9, Sep. 2018, Art. no. 2850.
- [35] H. Jansen, H. Gardeniers, M. De Boer, M. Elwenspoek, and J. Fluitman, "A survey on the reactive ion etching of silicon in microtechnology," *J. Micromech. Microeng.*, vol. 6, no. 1. pp. 14–28, 1996.

- [36] J. F. Buckwalter, X. Zheng, G. Li, K. Raj, and A. V. Krishnamoorthy, "A monolithic 25-Gb/s transceiver with photonic ring modulators and Ge detectors in a 130-nm CMOS SOI process," *IEEE J. Solid-State Circuits*, vol. 47, no. 6, pp. 1309–1322, Jun. 2012.
- [37] S. Meister *et al.*, "Matching p-i-n-junctions and optical modes enables fast and ultra-small silicon modulators," *Opt. Express*, vol. 21, no. 13, Jul. 2013, Art. no. 16210.
- [38] M. F. A. M. van Hest, M. S. Dabney, J. D. Perkins, D. S. Ginley, and M. P. Taylor, "Titanium-doped indium oxide: A high-mobility transparent conductor," *Appl. Phys. Lett.*, vol. 87, no. 3, Jul. 2005, Art. no. 032111.
- [39] H. Choi, M. Heuck, and D. Englund, "Self-similar nanocavity design with ultrasmall mode volume for single-photon nonlinearities," *Phys. Rev. Lett.*, vol. 118, no. 22, May 2017, Art. no. 223605.
- [40] S. Hu and S. M. Weiss, "Design of photonic crystal cavities for extreme light concentration," ACS Photon., vol. 3, no. 9, pp. 1647–1653, Sep. 2016.
- [41] M. R. Watts, W. A. Zortman, D. C. Trotter, R. W. Young, and A. L. Lentine, "Vertical junction silicon microdisk modulators and switches," *Opt. Express*, vol. 19, no. 22, Oct. 2011, Art. no. 21989.
- [42] J. Van Campenhout *et al.*, "Low-voltage, low-loss, multi-Gb / s silicon micro-ring modulator based on a MOS capacitor," in *Proc. Opt. Fiber Commun. Conf.*, 2012, pp. 10–12.
- [43] X. Xiao et al., "25 Gbit/s silicon microring modulator based on misalignment-tolerant interleaved PN junctions," Opt. Express, vol. 20, no. 3, Jan. 2012, Art. no. 2507.

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